FLUID DENSITY

Density is the ratio of mass to volume. In English, units density is expressed in pounds mass/cubic foot (lbm/ft³). The symbol for density is ρ . Density is usually written as:

 $\rho = lbm/ft^3$

The density for a liquid is normally taken from a table. Table 1 lists the densities of various liquids. For steam, the density is typically read from the steam tables for the desired pressure and temperature. For a gas, density is usually calculated using the ideal gas law. The ideal gas law is:

 $\rho = p/RT$

where p = pressure

R = gas constant

T = temperature

SPECIFIC VOLUME

Specific volume is the reciprocal of density and is the volume occupied by 1 lbm of fluid.

 $v = 1/\rho$

Table 2 gives the specific volume for saturated steam at various temperatures and pressures.

SPECIFIC GRAVITY

Specific gravity is the ratio of a fluid's density to some reference density. For liquids, the reference density is the density of pure water. Strictly speaking, specific gravity of a liquid cannot be given without specifying the reference temperature at which the water's density was evaluated. The density of water in English units is normally referenced at 32°F and is 62.43 lbm/ft³. Using this as the reference density, specific gravity is given as:

S.G. =
$$\frac{\text{density}}{62.431 \text{bm/ft}^3}$$

RELATIVE DENSITY

Relative density is the ratio of the density of one substance to that of another, both at the same temperature. The use of specific gravity to describe this quantity is discouraged, partially due to the fact there is no stipulation that the temperatures be equal in specific gravity measurements.

For gasses, the relative density is generally the ratio of the density of the gas to that of air, again both at the same temperature, and also at the same pressure and dryness.

Relative densities of petroleum products and aqueous acid solutions can be found using a device called a hydrometer. In addition to the hydrometer scale that references water, there are two basic hydrometer scales, the Baume scale and the API (American Petroleum Industry Scale). The Baume scale was widely used in the past but the API scale is now recommended for use with all liquids.

The API scale can be used with all liquids:

Relative Density = 141.5

131.5+°API

Table 3 lists the relative densities corresponding to the API scale.

For liquids lighter than water, their specific gravity can be found from the Baume hydrometer reading using this equation:

Relative Density =
$$\frac{140.0}{130.0+^{\circ}\text{Baume}}$$

For liquids heavier than water, their specific gravity can be found from the Baume hydrometer reading using this equation:

Relative Density =
$$\frac{145.0}{145.0^{\circ}\text{Baume}}$$

Relative densities can also be given for gases. The reference density is that of air at specified temperature and pressure. Since both the gas and air are evaluated at the same pressure and temperature, the relative density is the inverse of the ratio of the gas constants.

Timeta	Temperature	Density	Specific Gravity	
Liquia	F 64	10m/1t ^o	0.784	
Acetandenyde	60	48.9	0.784	
Acetone A cotio A phydride	68	49.4	1.092	
Acetic Annyande	08	67.5	1.083	
Acetic Acid (conc)	08	65.5	1.050	
Ammonia	10	40.9	0.656	
Aniine	08	63.8	1.023	
Benzene	32	56.1	0.899	
Benzoic Acid	59	/9.0	1.207	
Brine, 10% CaCl	32	68.1	1.091	
Brine, 10% NaCl	32	67.2	1.078	
Butyric Acid (conc)	68	60.2	0.965	
Carbon Disulfide	32	80.6	1.292	
Carbon Tetrachloride	68	99.6	1.597	
Chlorobenzene	68	69.1	1.108	
Chloroform	68	92.9	1.489	
Cresol, Meta	68	64.5	1.035	
Diphenyl	163	61.9	0.993	
Distillate	60	53.0	0.850	
Fuel Oil #6 (min)	60	61.9	0.993	
Furfural	68	72.3	1.160	
Gasoline	60	46.8	0.751	
Gasoline (natural)	60	42.4	0.680	
Glycerin	112	78.6	1.261	
Heptane	68	42.7	0.685	
Hydrochloric Acid (42.5%)	64	92.3	1.400	
Hydrocyanic Acid	64	43.5	0.697	
Kerosene	60	50.8	0.815	
Mercury	20	849.7	13.623	
	40	848.0	13.596	
	60	846.3	13.568	
	80	844.6	13.541	
	100	842.9	13.514	
Methylene Chloride	68	83.4	1.337	
Milk		64.2 - 64	.6	
Nitric Acid (conc)	64	93.7	1.502	
Olive Oil	59	57.3	0.919	
Ortho-phosphoric Acid	65	114.4	1.834	
Pentane	59	38.9	0.624	
Phenol	77	66.8	1.072	
Toluene	68	54.1	0.867	
Xylene	68	55.0	0.882	

TABLE 1 Density of Liquids

Pressure PSIA	Temp °F	Sp. Vol. ft ³ /lbm	Pressure PSIA	Temp °F	Sp. Vol. ft³/lbm	Pressure PSIA	Temp °F	Sp. Vol. ft³/lbm
0.50	79.58	641.4	80.0	312.03	5.472	250.0	400.95	1.8438
1.0	101.74	333.6	85.0	316.25	5.168	275.0	409.43	1.6804
2.0	126.08	173.73	90.0	320.27	4.896	300.0	417.33	1.5433
3.0	141.48	118.71	95.0	324.12	4.652	350.0	431.72	1.3260
4.0	152.97	90.63	100.0	327.81	4.432	400.0	444.59	1.1613
5.0	162.24	73.52	105.0	331.36	4.232	450.0	456.28	1.0320
10.0	193.21	38.42	110.0	334.77	4.049	500.0	467.01	0.9278
14.7	212.00	26.80	115.0	338.07	3.882	550.0	476.93	0.8422
15.0	213.03	26.29	120.0	341.25	3.728	600.0	486.21	0.7698
20.0	227.96	20.089	125.0	344.33	3.587	650.0	494.90	0.7085
25.0	240.07	16.303	130.0	345.32	3.455	700.0	503.10	0.6554
30.0	250.33	13.746	135.0	350.21	3.333	750.0	510.85	0.6094
35.0	259.28	11.898	140.0	353.02	3.220	800.0	518.23	0.5687
40.0	267.25	10.498	145.0	355.76	3.114	850.0	525.26	0.5328
45.0	274.44	9.401	150.0	358.42	3.015	900.0	531.98	0.5006
50.0	281.01	8.515	160.0	363.53	2.834	950.0	538.42	0.4718
55.0	287.07	7.787	170.0	368.41	2.675	1000	544.61	0.4456
60.0	292.71	7.175	180.0	373.06	2.532	1250	572.42	0.3450
65.0	297.97	6.665	190.0	377.51	2.404	1500	596.23	0.2765
70.0	302.92	6.206	200.0	381.79	2.288	1750	617.09	0.2267
75.0	307.60	5.816	225.0	391.79	2.042	2000	635.82	0.1878

TABLE 2 Properties of Saturated Steam

TABLE 3 Relative Density at 60°/60°F Corresponding to the API Scale

Degree API	Relative Density	Pound US Gal.	Degree API	Relative Density	Pound US Gal.	Degree API	Relative Density	Pound US Gal.
10	1.0000	8.328	41	0.8203	6.830	71	0.6988	5.817
11	0.9930	8.270	42	0.8155	6.790	72	0.6953	5.788
12	0.9861	8.212	43	0.8109	6.752	73	0.6919	5.759
13	0.9792	8.155	44	0.8063	6.713	74	0.6886	5.731
14	0.9725	8.099	45	0.8017	6.675	75	0.6852	5.703
15	0.9659	8.044	46	0.7972	6.637	76	0.6819	5.676
16	0.9593	7.989	47	0.7927	6.600	77	0.6787	5.649
17	0.9529	7.935	48	0.7883	6.563	78	0.6754	5.622
18	0.9465	7.882	49	0.7839	6.526	79	0.6722	5.595
19	0.9402	7.830	50	0.7796	6.490	80	0.6690	5.568
20	0.9340	7.778	51	0.7753	6.455	81	0.6659	5.542
21	0.9279	7.727	52	0.7711	6.420	82	0.6628	5.516
22	0.9218	7.676	53	0.7669	6.385	83	0.6597	5.491
23	0.9159	7.627	54	0.7628	6.350	84	0.6566	5.465
24	0.9100	7.578	55	0.7587	6.316	85	0.6537	5.440
25	0.9042	7.529	56	0.7547	6.283	86	0.6506	5.415
26	0.8984	7.481	57	0.7507	6.249	87	0.6476	5.390
27	0.8927	7.434	58	0.7467	6.216	88	0.6446	5.365
28	0.8871	7.387	59	0.7428	6.184	89	0.6417	5.341
29	0.8816	7.341	60	0.7389	6.151	90	0.6388	5.316
30	0.8762	7.296	61	0.7351	6.119	91	0.6360	5.293
31	0.8708	7.251	62	0.7313	6.087	92	0.6331	5.269
32	0.8654	7.206	63	0.7275	6.056	93	0.6303	5.246
33	0.8602	7.163	64	0.7238	6.025	94	0.6275	5.222
34	0.8550	7.119	65	0.7201	5.994	95	0.6247	5.199
35	0.8498	7.076	66	0.7165	5.964	96	0.6220	5.176
36	0.8448	7.034	67	0.7128	5.934	97	0.6193	5.154
37	0.8398	6.993	68	0.7093	5.904	98	0.6160	5.131
38	0.8348	6.951	69	0.7057	5.874	99	0.6139	5.109
39	0.8299	6.910	70	0.7022	5.845	100	0.6112	5.086
40	0.8251	0.870						

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ACFM vs. SCFM

It is often desirable to express a gas flow in terms of a "standard" volumetric flowrate. One of the most common forms encountered is standard cubic feet per minute (scfm). To convert an actual flowrate reading, here referred to as actual cubic feet per minute (acfm), it is necessary to multiply the actual flowrate by the ratio of the standard condition's specific volume over the actual condition's specific volume.

 $Q_{s} = Q_{A} [v_{s} / v_{A}]$

where: $Q_s =$ flowrate in scfm

 $Q_A =$ flowrate in acfm

 $v_{\rm s}$ = standard conditions specific volume

 v_{A} = actual conditions specific volume

The ratio v_s / v_A can be written as:

 $[T_sP_A/P_sT_A]$

IDEAL GAS BEHAVIOR

A gas can be considered ideal if it exhibits ideal gas behavior. Typically, gases at low pressures and at temperatures much higher than their critical temperatures can be treated as ideal gases. When the volume occupied by the gas molecules is negligible in comparison to the total volume, it is acceptable to treat the gas as an ideal gas. The benefit of treating gases as ideal is that it greatly simplifies the math required to evaluate their behavior.

There are two basic laws that define the behavior of ideal gases; they are Boyle's and Charle's Law. Boyle's law states that the volume and pressure of an ideal gas vary inversely when the temperature is held constant and is written as:

$$\mathbf{p}_1 \mathbf{V}_1 = \mathbf{p}_2 \mathbf{V}_2$$

The second law is Charle's law that states when pressure is held constant, volume and temperature vary proportionally. Charle's law is written:

$$\frac{\mathbf{T}_1 = \mathbf{T}_2}{\mathbf{V}_1 \ \mathbf{T}_2}$$

The ideal gas law relates the pressure, temperature, and volume to the amount of gas present. The ideal gas law states that equal volumes of different gases at the same temperature and pressure contain the same number of molecules. The ideal gas law is written:

$$pV = nR*T$$

R* is known as the universal gas constant. It is universal because the same number can be used with any gas. Due to the different units that can be used for pressure, temperature, and volume, there are different values of R*. Table 4 lists values for R*.

The ideal gas law can be used with more than 1 mole of gas. If there are n moles, the equation is written as:

$$n = m/M$$

TABLE 4 Values of Universal Gas Constant

1545.33	ft-lbf/pmole-°R
0.08206	atm-liter/gmole-°K
1.986	BTU/pmole-°R
1.986	cal/gmole-°K
8.314	joule/gmole-°K
0.730	atm-ft3/pmole-°R

The ideal gas law can be rewritten taking into account the molecular weight of the specific gas. The specific gas constant is unique for each gas.

$$pV = mR*t/M$$

 $pV = mT(R*/M)$
 $pV = mRT$

Table 5 lists the properties of common gases.

Since density is the reciprocal of specific volume, the ideal gas law can be used to determine the density of an ideal gas. If m=1, then the ideal gas law can be rewritten as:

$$p = \frac{1RT}{v}$$
$$p = RT$$
$$\rho = \frac{p}{RT}$$

PROPERTIES OF REAL GASES

Unfortunately, it is not always possible to achieve acceptable results by using the ideal gas law. It is very common for gases at low temperatures and/or high pressures to exhibit real gas behavior.

When the spacing between the gas molecules is small, they tend to attract each other. These attractive forces are called Van der Waals forces. Van der Waal's equation of state can be used to describe the behavior of real gases. Van der Waal's equation of state is written as:

$$(\underline{p+a})(V-b) = nR*T$$

$$V^{2}$$

For an ideal gas, a and b are zero and Van der Waal's equation reduces to the familiar ideal gas law.

Since real gas molecules tend to attract each other, the actual pressure exerted by a real gas is less than that predicted by the ideal gas law. The reduction in pressure is corrected for in the Van der Waal equation by the term (a/V2). The constant b is dependent on the volume occupied by the gas molecules in the dense state. Table 6 gives the values for a and b of common gases. The Van der Waal equation is typically used only when the gas is below critical pressure.

Gas	Symbol	MW	R	Density	k
Acetylene	C ₂ H ₂	26.0	59.4	0.07323	1.30
Air		29.0	53.3	0.08071	1.40
Ammonia	NH ₂	17.0	91.0	0.04813	1.32
Argon	A	39.9	38.7	0.11135	1.67
Carbon Dioxide	CO	44.0	35.1	0.12341	1.28
Carbon Monoxide	CO ²	28.0	55.2	0.07806	1.40
Chlorine	Cl ₂	70.9	21.8	0.2006	1.33
Ethane	C,H	30.07	51.3	0.08469	1.18
Ethylene	$C_2 H_4^0$	28.0	55.1	0.07868	1.22
Freon (R-12)	CĈl,̂F,	120.9	12.6		1.13
Helium	He ²	4.0	386.3	0.01114	1.66
Hydrogen	H ₂	2.0	766.8	0.00561	1.41
Isobutane	$C_{4}H_{10}$	58.12	26.6		1.09
Krypton	Kr	82.9	18.6	0.2315	1.67
Methane	CH_{4}	16.0	96.4	0.04475	1.32
Neon	Ne	20.18	76.4	0.05621	1.64
Nitrogen	N ₂	28.0	55.2	0.07807	1.40
Oxygen	O_2^2	32.0	48.3	0.08921	1.40
Propane	C ₃ H ₈	44.09	35.0	0.1254	1.12
Steam**	H ₂ O [°]	18.0	85.8		1.28
Sulfur Dioxide	SÔ,	64.1	24.0	0.1827	1.26
Xenon	Xe	130.2	11.9		1.67

TABLE 5 Properties of Common Gases

** Values for steam are approximate and may be used only for low pressures and high temperatures. *R* is in ft-lbf/lbm- $^{\circ}$ R, Density is in lbm/ft³ at 32 $^{\circ}$ F and 14.7 PSIA.

TABLE 6 Values of a and b for Common Gases

	a(atm-ft ⁶ /pmole)	b(ft³/pmole)
Air	345.2	0.585
CO_2	926	0.686
H_2	62.8	0.427
O_2	348	0.506
Steam	1400	0.488

There is another correction factor that is applied to real gases. This factor is known as the compressibility factor, and is sometimes used for correction of gas flows through orifices. The compressibility factor is denoted by Z, and is dependent on pressure, temperature, and the type of gas. The modified ideal gas law is:

pV = ZRT

Correction factors for gases can be plotted against pressure and temperature. By using the principle of corresponding states, it is possible to create one graph that covers multiple gases. The principle of corresponding states says that all gases behave alike whenever they have the same reduced variables. The reduced variables that the law refers to are the ratios of pressure, temperature, and volume to their critical values. Table 7 gives critical properties for selected gases.

$$P_{r} = P/P_{c}$$
$$T_{r} = T/T_{c}$$
$$V_{r} = v/v_{c}$$

 TABLE 7
 Approximate Critical Properties

gas	$T_{c}(^{\circ}R)$	P _c (psia)
Air	235.8	547.0
Ammonia	730.1	1639.0
Argon	272.2	705.0
Carbon Dioxide	547.8	1071.0
Carbon Monoxide	242.2	508.2
Chlorine	751.0	1116.0
Ethane	549.8	717.0
Ethylene	509.5	745.0
Helium	10.0	33.8
Hydrogen	60.5	188.0
Mercury	2109.0	2646.0
Methane	343.9	673.3
Neon	79.0	377.8
Nitrogen	227.2	492.5
Oxygen	278.1	730.9
Propane	666.3	617.0
Sulfur Dioxide	775.0	1141.0
Water Vapor	1165.4	3206.0
Xenon	521.9	855.3





FIGURE 1 Compressibility Factors for Low Pressure as presented by Professor E. Obert and L. Nelson in "Generalized P-V-T Properties of Gases," ASME Transactiona, 76, 1057 (1954)



FIGURE 2 Compressibility Factors for High Pressure

VISCOSITY

The viscosity of a liquid is a measure of its resistance to flow. Liquids can be categorized by their viscosity properties. One of the most common liquid categories is Newtonian liquids.

Viscosity is measured using two parallel plates and a layer of fluid. The plates are separated from each other by a layer of fluid with a thickness of y. One plate is fixed and the other one is maintained at a constant velocity by a constant force F.

It has been shown that for Newtonian fluids, the force required to maintain the velocity is proportional to the velocity and inversely proportional to the separation of the plates.

F	= dv
A	dy

The constant of proportionality is the absolute viscosity. The quantity F/A is the shear stress in the fluid. The equation can be written as:

 $t = u(dv/dy) \rho$

Kinematic viscosity is also used commonly and is a combination of absolute viscosity and the density of the fluid.

$$v = ug/\rho$$

Tables 8 and 9 give conversion factors for the most commonly encountered viscosity units.

TABLE 8 Equivalents of Absolute Viscosity

Absolute Viscosity	Centipoise	Poise	<u>Pound</u> Ft Sec
Centipoise	1	0.01	0.000672
Poise	100	1	0.0672
<u>Pound</u> Ft Sec	1487	14.87	1

TABLE 9 Equivalents of Kinematic Viscosi	Kinematic Viscosity
--	---------------------

Kinematic Viscosity	Centistoke	Stoke	<u>Ft²</u> Sec
Centistoke	1	0.01	0.00001076
Stoke	100	1	0.001076
$\frac{Ft^2}{Sec}$	92,900	929	1

Table 10 lists the viscosity of common liquids and Table 11 lists the viscosity of common gases.

Temperature	Viscosity	Temperature	Viscosity	Temperature	Viscosity
°F	Centipoise	°F	Centipoise	°F	Centipoise
Acetic A	cid	Ethylene	e Oxide	Isohexar	ie
59	1.31	-57	0.577	32	0.376
64	1.30	-37	0.488	68	0.306
77	1.155	-5.8	0.394	104	0.254
86	1.04	32	0.320	Isopenta	ne
106	1.00	Fluorber	izene	32	0.273
212	0.43	68	0.598	68	0.223
Acetic A	nhvdride	140	0.389	Kerosen	e
32	1.24	212	0.275	68	2.69
59	0.971	Fuel Oil	, #2	100	2.0
64	0.90	70	3.0 - 7.4	Methyl A	Alcohol
86	0.783	100	2.11 - 4.28	-48	1.98
212	0.490	Fuel Oil	,#6	32	0.82
Acetone		122	97.4 - 660	59	0.623
14	0.450	160	37.5 - 172	68	0.597
32	0.399	Gasoline		77	0.546
59	0.337	60	0.46 - 0.88	86	0.510
77	0.316	100	0.40 - 0.71	Methyl C	Chloride
Ammoni	a	Glycerin		0	0.25
-92	0.475	32	12,110	20	0.23
-58	0.317	43	6,260	40	0.21
-40	0.276	59	2,330	60	0.19
-28	0.255	68	1,490	100	0.16
Benzene		77	954	Naphtha	lene
32	0.912	86	629	176	0.967
50	0.758	Heptane		212	0.776
68	0.652	32	0.524	Nitric Ac	cid
86	0.564	63	0.461	32	2.275
104	0.503	68	0.409	Nitroben	izene
122	0.542	77	0.386	37	2.91
Carbon 7	etrachloride	104	0.341	42	2.71
32	1.329	Hexane		50	2.48
59	1.038	32	0.401	68	2.03
68	0.969	68	0.326	Nitrome	thane
86	0.843	77	0.386	32	0.853
104	0.739	104	0.341	77	0.620
140	0.585	Hyrdoch	loric Acid, 31.5%	n-Octane	e
Chlorine	Liquid	0	3.4	32	0.706
-40	0.505	20	2.9	68	0.240
-20	0.462	40	2.5	104	0.433
20	0.400	60	2.0	Pentane	
60	0.350	80	1.8	32	0.289
100	0.313	100	1.6	68	0.524
Ethylben	zene	140	1.2	Phenol	
63	0.691	Iodine L	iquid	65	12.7
Ethylene	Glycol	241	2.27	122	3.49
68	19.9	Isohepta	ne	158	2.03
104	9.13	32	0.481	194	1.26
140	4.95	68	0.384		
176	3.02	104	0.315		

TABLE 10 Viscosity of Common Liquids

(continued)

Temperature °F	Viscosity Centipoise	Temperature °F	Viscosity Centipoise	Temperature °F	Viscosity Centipoise
Phosphorus Liquid		Sodium Liquid		Sulfuric Acid	
71	2.34	0	2.4	32	48.4
88	2.01	26	1.3	59	32.8
110	1.73	40	1.2	68	25.4
123	1.60	60	1.1	86	15.7
140	1.45	100	1.0	104	11.5
158	1.32	140	0.85	104	0.02
Sodium Hydroxide		Sulfur (gas free)		122	0.02 7.00
70	100	253	10.9	140 T	1.22
100	40	255	9 7	Turpentine	
120	25	270	0.7	60	2.11
140	15	301	7.1	100	2.0
160	9.5	314	7.2	Water	
200	3.7	317	7.6	60	1.13
220	2.4	319	14.5	130	0.55
250	1.4	Sulfur Dioxide		150	0.00
		-28	0.5508		
		13	0.4285		
		32	0.3936		

TABLE 10 Viscosity of Common Liquids (continued)

Temperature °F	Viscosity Centipoise	Temperature °F	Viscosity Centipoise	Temperature °F	Viscosity Centipoise
Acetylene		Carbon Monoxide		Nitrogen	
32	0.00935	32	0.0166	-6.7	0.0156
Air		59	0.0172	51.6	0.0171
32	0.0171	260.8	0.0218	81	0.0178
104	0.0190	Chlorine		261	0.0219
444	0.0264	122	0.0147	440	0.0256
633	0.0305	212	0.0168	Oxygen	
674	0.0312	302	0.0187	32	0.0189
768	0.0341	392	0.0208	67	0.0202
Ammonia		Ethane		262	0.0257
32	0.0092	32	0.0085	440	0.0302
68	0.0098	63	0.0090	n-Pentane	
212	0.0128	Ethylene		77	0.0068
302	0.0146	32	0.0091	212	0.0084
482	0.0181	68	0.0101	Propane	
Argon		122	0.0110	64.2	0.0079
32	0.0210	212	0.0126	213	0.0101
68	0.0222	Helium		Propylene	
212	0.0269	32	0.0186	62	0.0083
392	0.0322	68	0.0194	122	0.0093
Benzene		Hydrogen		Sulfur Dioxide	
0	0.0065	-172	0.0057	32	0.0116
40	0.0070	-143.5	0.0062	64.4	0.0124
70	0.0075	-25	0.0077	68.9	0.0125
100	0.0080	32	0.0084	213	0.0161
200	0.0091	69	0.0088		
Butene		264	0.0108		
0	0.0075	Hydrogen Chloride			
40	0.0080	54.4	0.0139		
70	0.0085	61.8	0.0141		
100	0.0090	212	0.0182		
200	0.0104	Hydrogen Sulfide			
Butylene		32	0.0117		
66	0.0074	62.6	0.0124		
212	0.0095	212	0.0159		
Carbon Dioxide		Methane	0.0100		
-144	0.0090	32	0.0102		
-76	0.0106	68	0.0109		
32	0.0139	212	0.0133		
68	0.0148				
86	0.0153				

TABLE 11 Viscosity of Common Gases

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Reference

Reference











Reference